

Aggregation

- Need to aggregate impacts across individuals
- Welfare Function: Aggregation of individual welfare functions.

Individual welfare function for i

- $U_i = U_i(X_{i1}, X_{i2}, \dots, X_{ij})$
- $\text{Max } L = U_i(X_{i1}, X_{i2}, \dots, X_{ij})$
 $\quad - \lambda (p_1 * X_{i1} + p_2 * X_{i2} \dots - Y)$
- FOC:
 - $\partial U_{ij} / \partial X_j = \lambda * P_j$
 - $\partial U_{ij} / \partial X_j = \partial U_i / \partial Y * P_j$
- $dU_i = \sum_j \partial U_i / \partial X_j dX_{ij} = \sum_j \partial U_i / \partial Y * P_j dX_{ij}$

Social Welfare Function

- $W = W(U_1, U_2, U_3, \dots, U_n)$
- $dW = \sum_i \partial W / \partial U_i dU_i$
 $= \sum_j \sum_i \partial W / \partial U_i * \partial U_i / \partial Y * P_j dX_{ij}$
 $= MSU_i * MU \text{ Income}_i * P_j dX_{ij}$

Kaldor – Hicks Compensation Tests

- Kaldor: The winners from a project can *in principle* compensate the losers
- Hicks: The losers cannot bribe the potential winners *not to* undertake the project
- Scitovsky: Both the Kaldor and Hicks criteria are met.

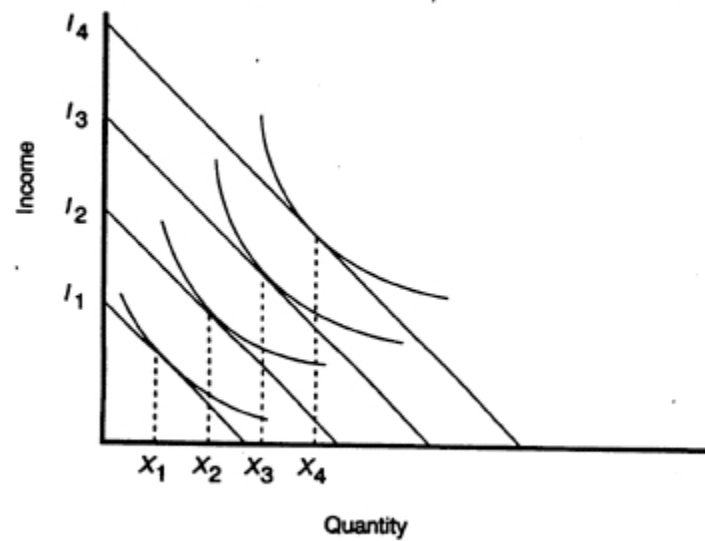
Kaldor – Hicks Compensation Tests

- These compensation tests assume:
 - $MSU_i = MSU_j$ for all i, j
 - $MU_i \text{ Income} = MU_j \text{ Income} = k$.
- A dollar has the same “value” (utility) for all individuals in society, no matter what their income level (or other characteristics).

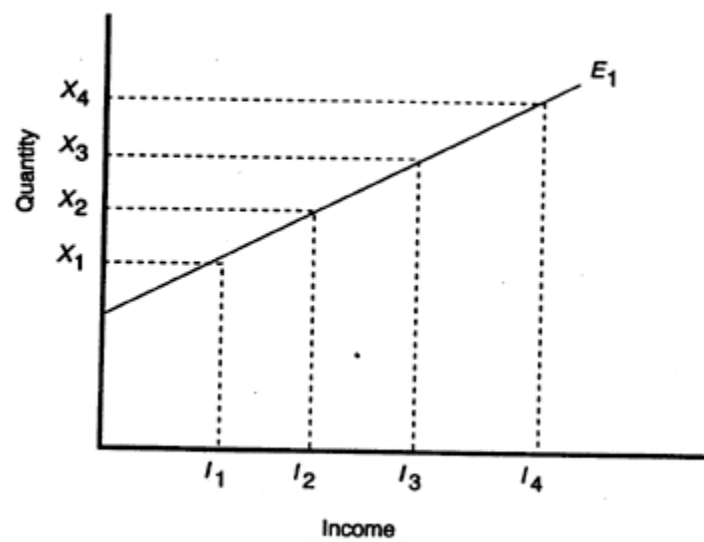
Gorman Demand form

- $U_i = A_i(P) + B(P) * Y_i$
- $\partial U_i / \partial Y = B$ (for all i)

Figure 6.1 Gorman form Engle curves.



(a)



(b)

Example from Zerbe & Dively

- Consider option to build an airport
- Impacts:
- Costs
 - If built, neighboring residents will suffer from increased noise
 - WTP to not have the airport built (EV)
 - WTA after airport is built (CV)
- Benefits
 - Airlines “gain” from airport (increased profits)

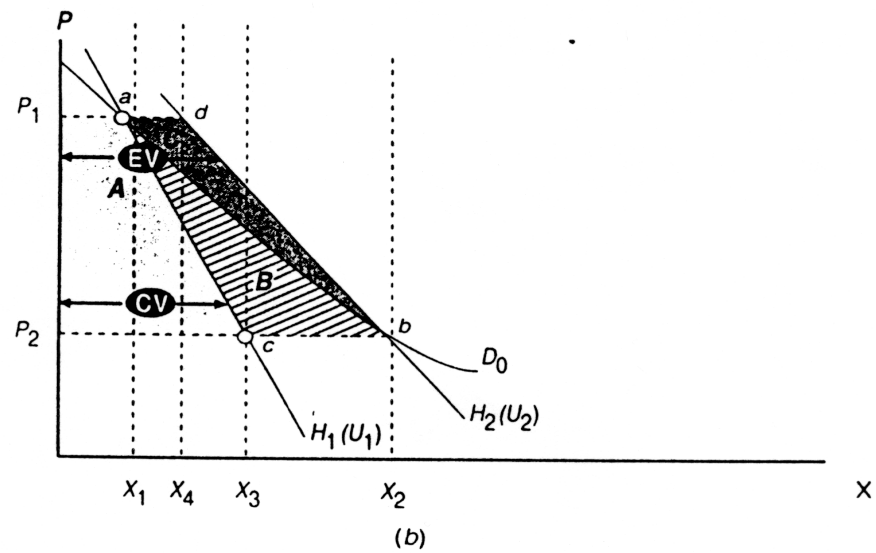
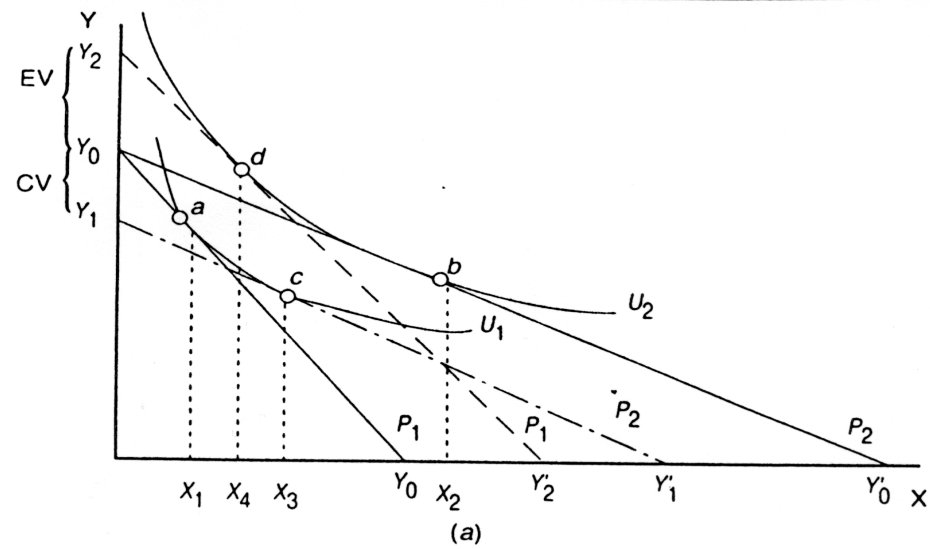
Example 1

	Residents	Airlines	Net Social Value
No airport to airport	-5000 WTA	+3000 WTP	-2000 Kaldor
Airport to no airport	+3500 WTP	-3000 WTA	+500 Hicks

WTP vs WTA

- Generally Expect WTP to avoid a negative change will be less than the WTA to accept the change.
- Why?
 - WTP is constrained by limited income
 - WTA is unconstrained
- For normal goods, price reduction will have positive income effect, price increase will have negative income effect

FIGURE 5.8 CV, EV, and compensated demand curves.



Question?

- Why would airlines (firms) have different WTP than WTA?
 - WTP should be equal to expected future profits
 - WTA should also be equal to expected future profits
- General point – always need to look at final impacts on *consumers*

Alternative Formulation

- Rather than the “benefits” of the airlines, consider the benefits of building the airport to local residents who would be able to use the new airport:
 - Reduced (total) price of airline travel (including the price of travel to the nearest airport)

Example 1

	Residents	Airlines	Net Social Value
No airport to airport	-5000 WTA	+3000 WTP	-2000
Airport to no airport	+3500 WTP	-3000 WTA	+500

Example 1A

	Residents	Resident airline travelers	Net Social Value
No airport to airport	-5000 WTA	+2000 WTP	-3000
Airport to no airport	+3500 WTP	-3200 WTA	+300

Ambiguous Outcomes of Compensation Rules

Example 2

	Residents	Resident airline travelers	Net Social Value
No airport to airport	-5000 WTA	+2000 WTP	-3000
Airport to no airport	+3500 WTP	-4000 WTA	-500

Ambiguous Outcomes of Compensation Rules

- In this situation:
 - If airport does not exist, don't build it
 - If airport exists, do not get rid of it
- *"Tyranny of the Status Quo"*
- Also, depends on property rights.
 - Do residents have right to quiet. If so they do not have pay the passengers, but passengers must compensate the residents for noise created.